

Teaching with Technology: Apps and Innovation in the Maths Classroom

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Overview:

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Context

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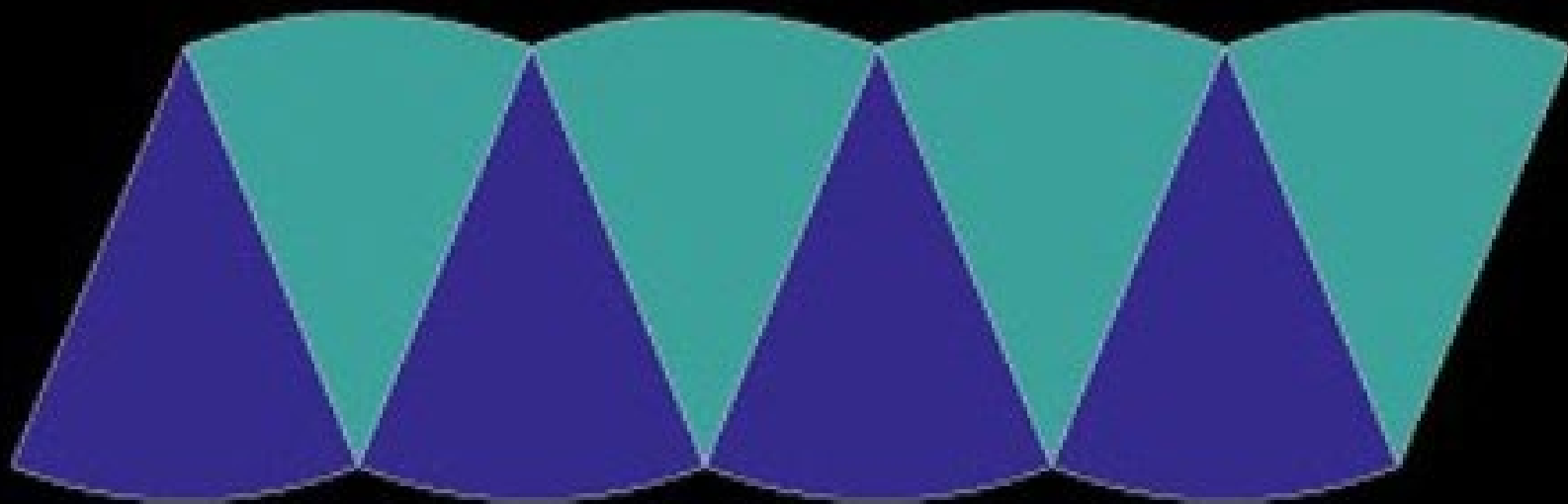
Background

3

Motivation

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$$\text{Area} = \pi r^2$$



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How do
you start
your
classes?



Technology in the classroom: Purpose

- No matter the teaching strategy, every strategy we use has a purpose.
- It is the purposeful integration of technology that enables us to transform our teaching.
- Technology provides alternative strategies for engaging and working with students and supporting teaching and learning in the classroom.
- The goal is **not** to use technology to tick a box.

Question: How do you identify the purpose?

Technology in the classroom: Understanding

- What do we do well?
- What are the challenges that we face?
- What would we like to do better?
- Conceptual understanding versus 'just memorise this'.

Question: How can we effectively use technology in the classroom to develop students' understanding?

Technology in the classroom: Why?

- Technology enables alternative ways of engaging with a concept.
- Dynamic and responsive interactions with mathematics.
- Enables us to ask 'What if...' and then test our ideas to determine their truth.
- Promotes student engagement by repositioning students as equal participants in meaning construction.
- Promotes mathematical conversations by reducing the barriers to entry.

Technology in the classroom: Goal

- To develop resources that engage students and enable mathematical conversations to happen.
- To provide multiple representations so that students of all abilities can engage meaningfully in mathematics.
- Position students to construct meaning for themselves. Enable them to 'discover' as opposed to being told.

Consider the following:

- Questioning can be used to guide students towards understanding.
- Examples of questioning strategies used to engage students and promote thinking:
 - "What do you observe/notice about...?"
 - "Does anyone notice any patterns?"
- Positioning students to develop their own understanding. Students can actively participate in meaning construction.
- Discussions about mathematics and ideas enables students of all abilities to participate.
- Engage students' and teachers' natural curiosity. Encourage students to ask 'Why?'.

Reflections in the plane

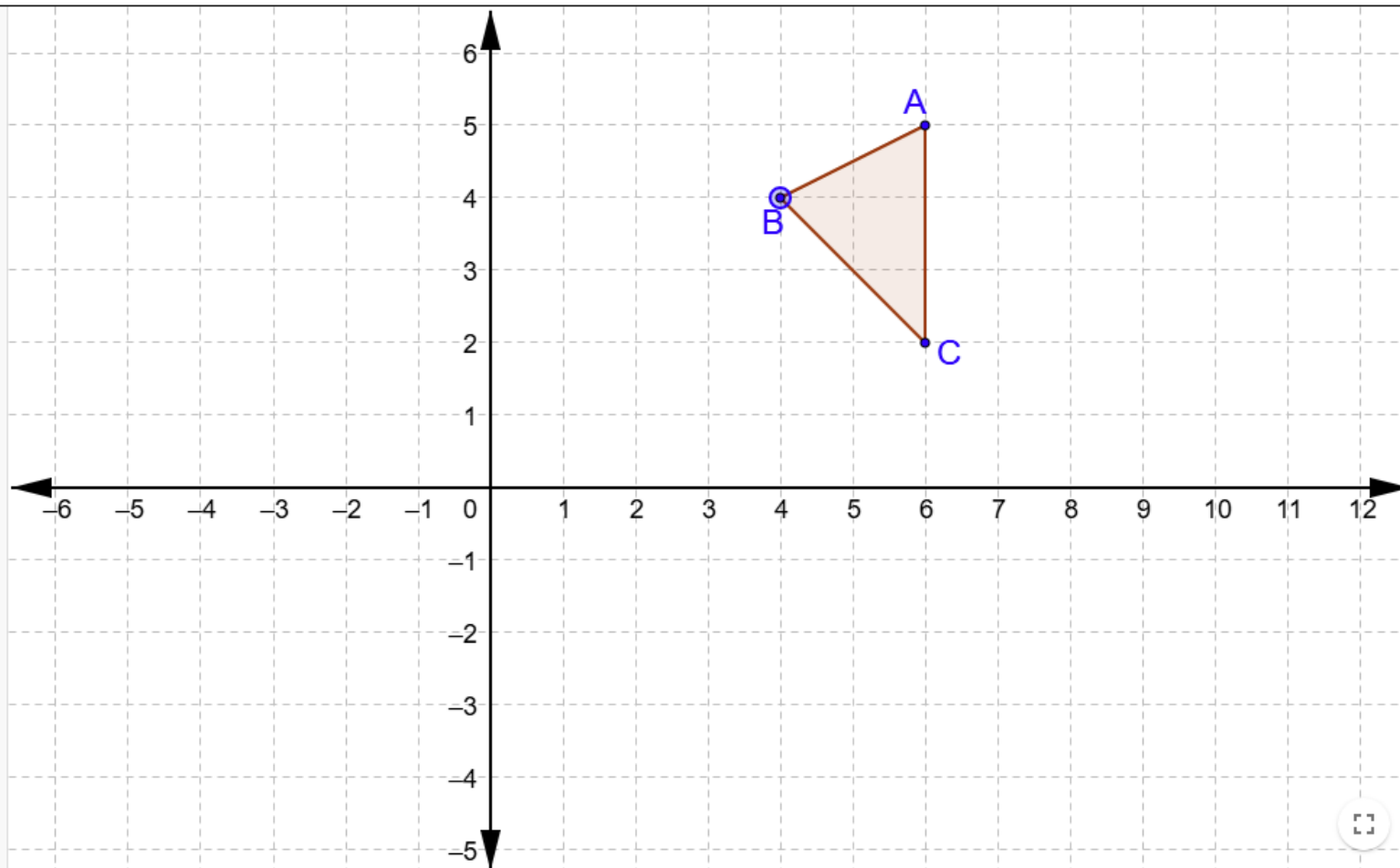
GeoGebra: <https://www.geogebra.org/m/EmmRE5Kk>

Reflections

Vertical Line

Horizontal Line

$y=x$



Similarity and Congruence: Is there another way?

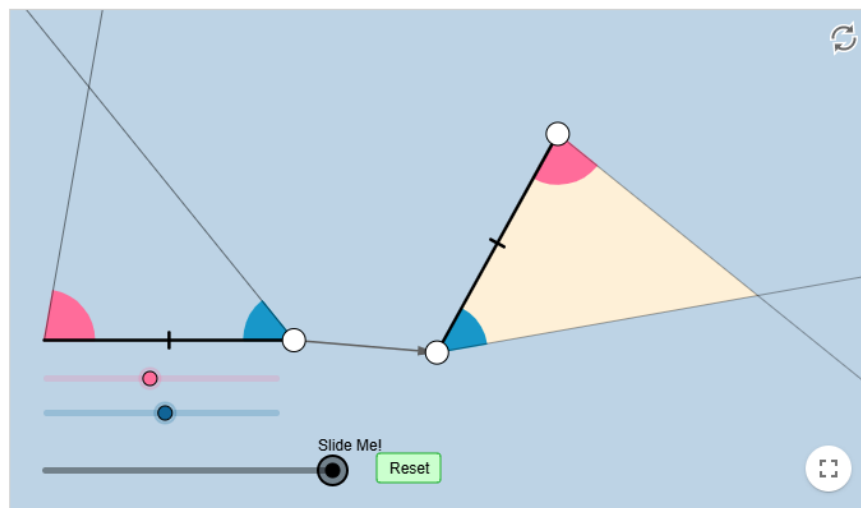
GeoGebra: <https://www.geogebra.org/m/mmEVNZHK>

ASA Theorem?

Author: [Tim Brzezinski](#)

Suppose 2 triangles have 2 pairs of congruent angles. Suppose we also know that the side between each set of given angles (in one triangle) is congruent to the side between this same pair of angles in the other triangle.

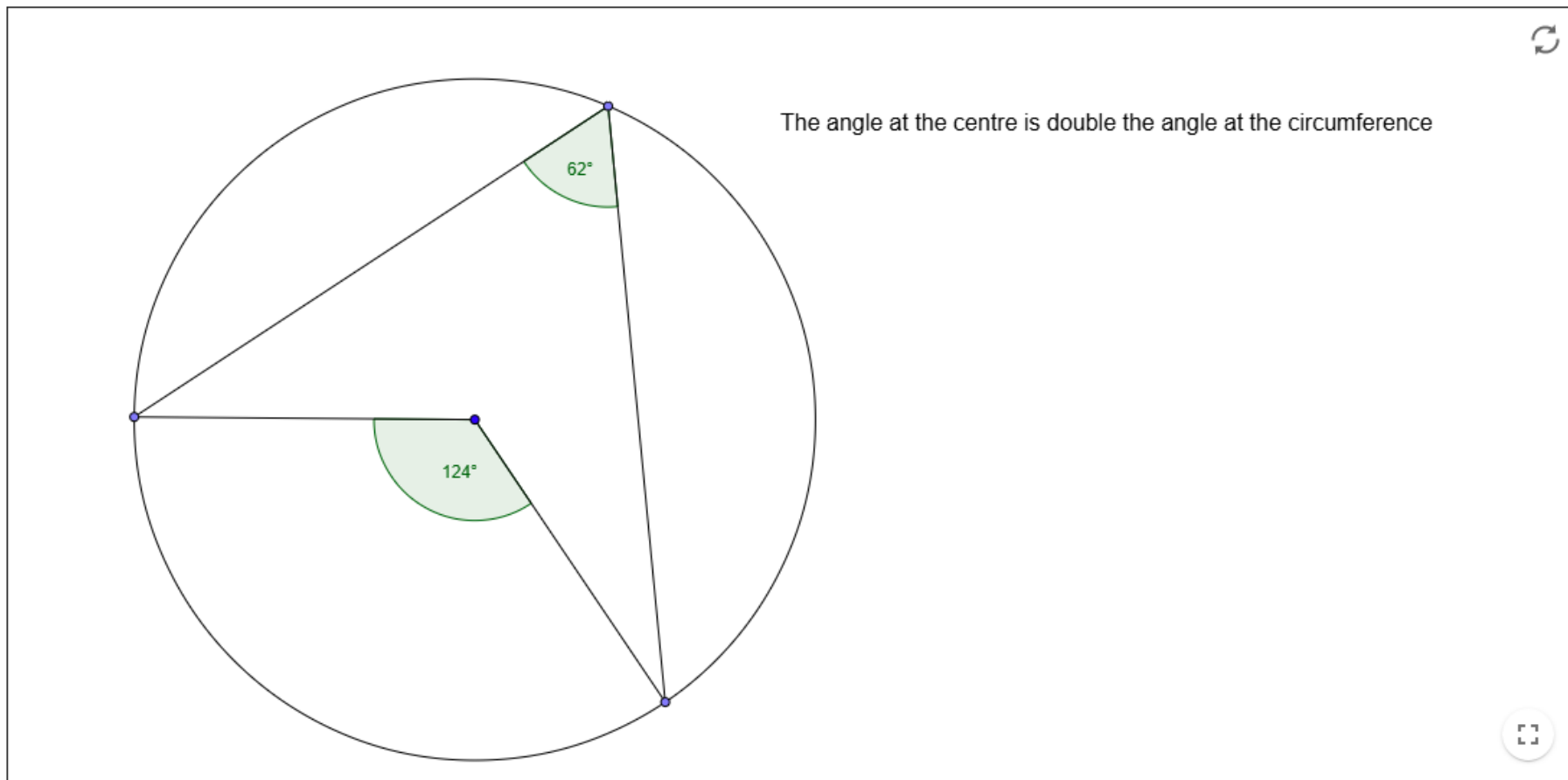
Does knowing only this constitute sufficient evidence to prove the triangles congruent? If so, explain how/why with respect to the transformations and/or triangle congruence theorems you've previously learned. If not, clearly explain why not.



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Circle Geometry: How to prove?

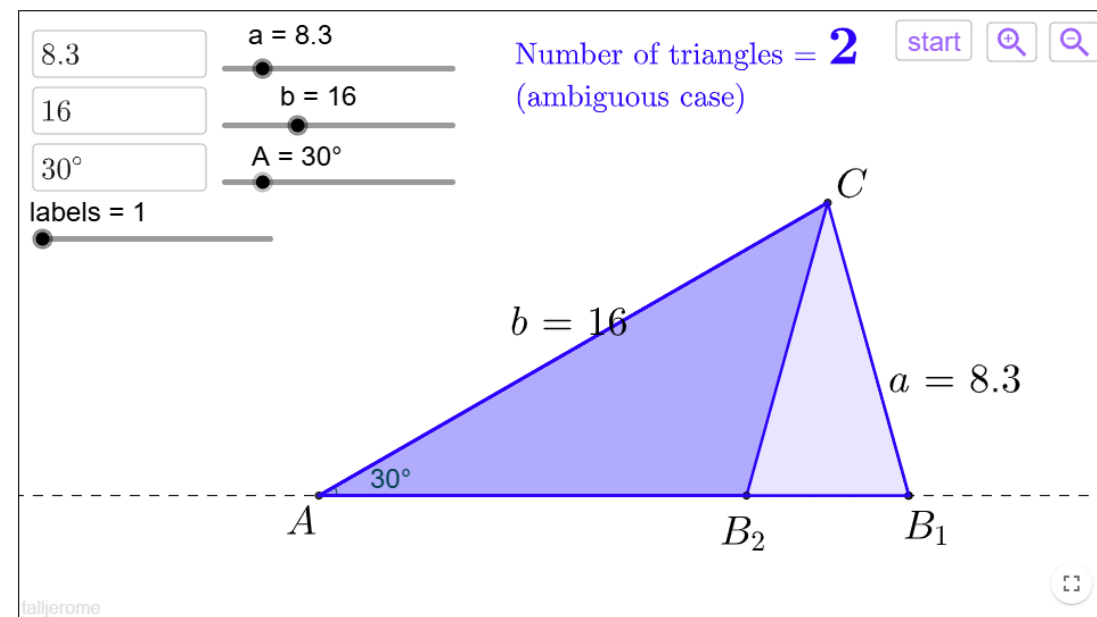
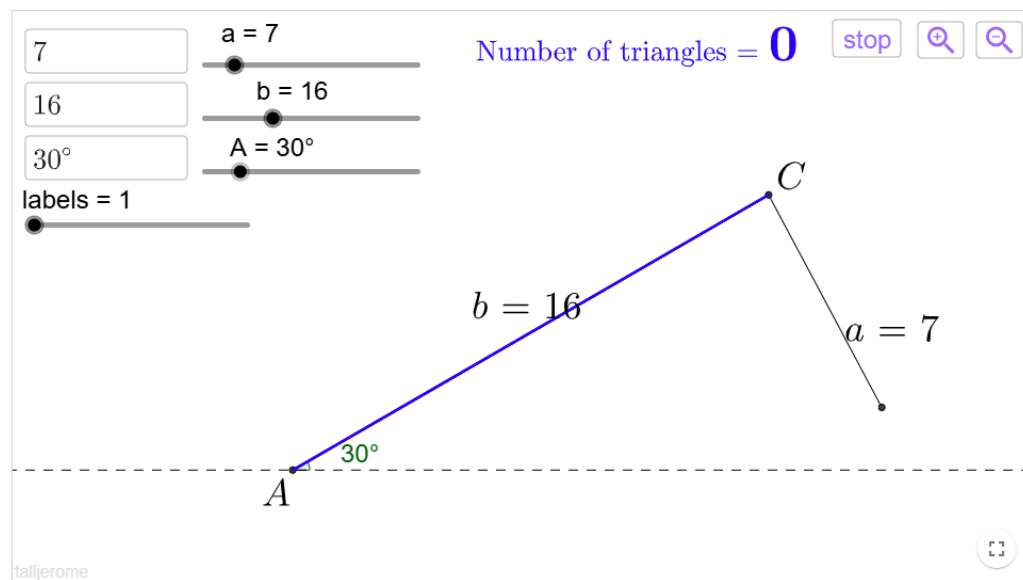
GeoGebra: <https://www.geogebra.org/m/EzaeAWNH>



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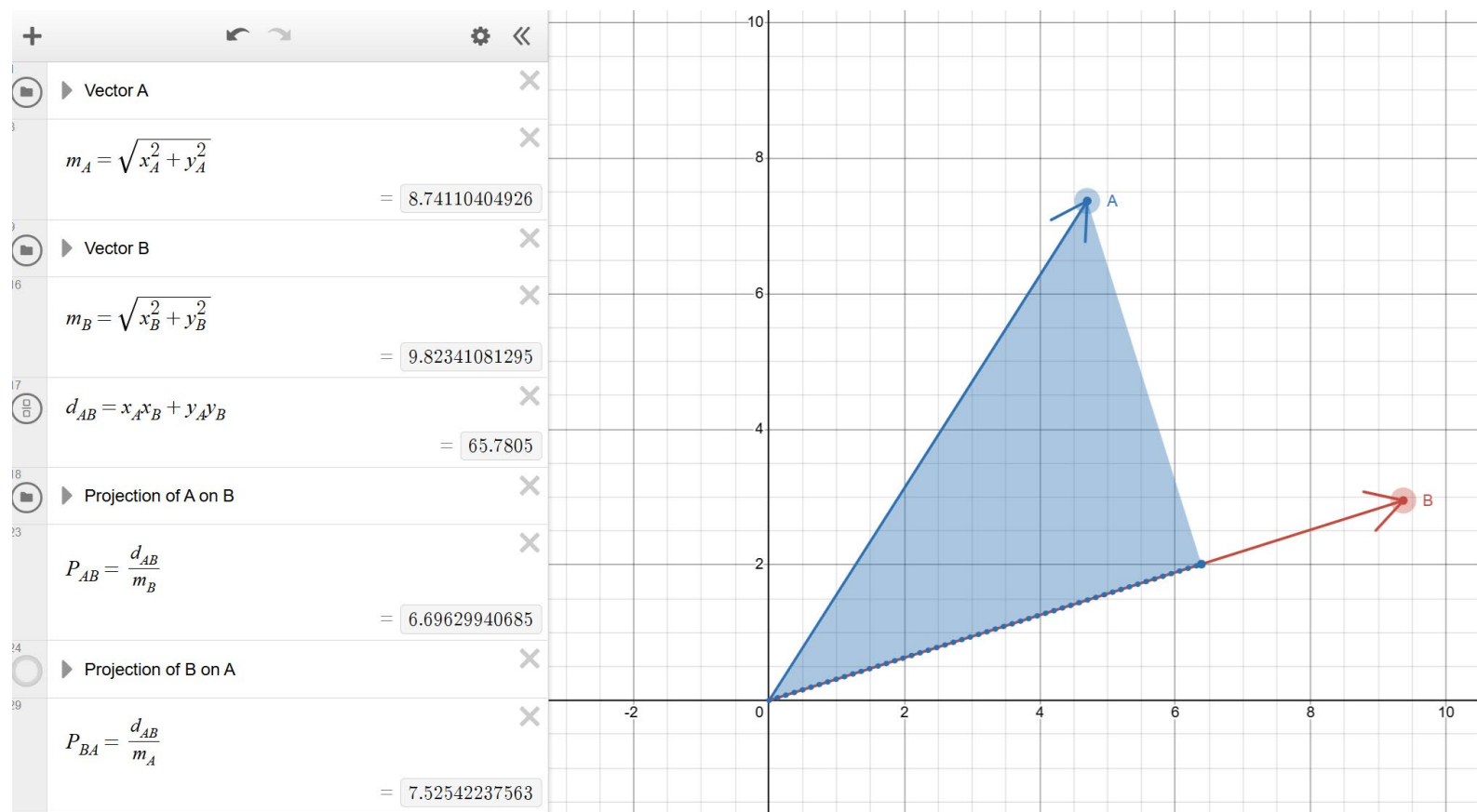
Sine rule: Ambiguous no more?

GeoGebra: <https://www.geogebra.org/m/CvtskyRM5>



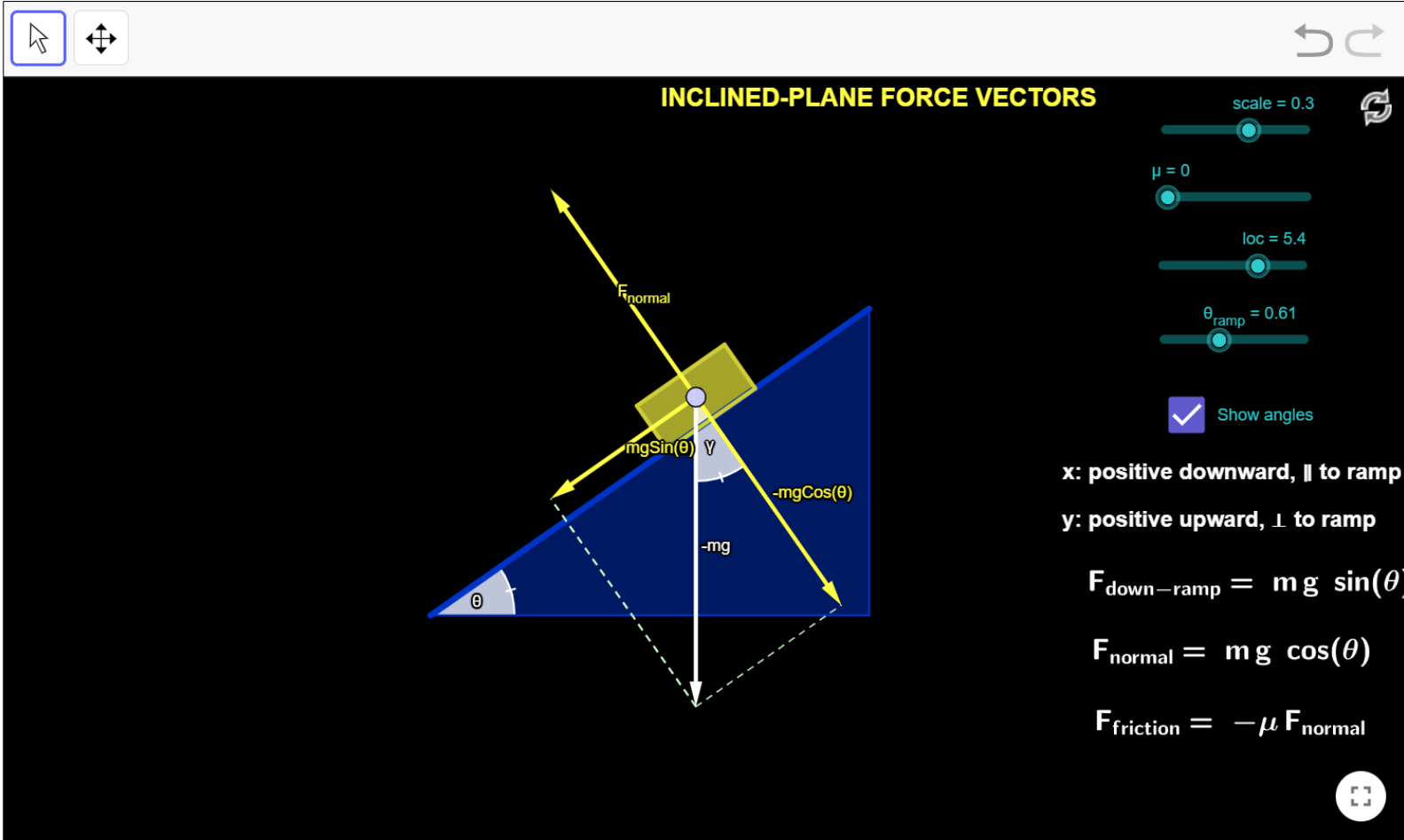
Vector Resolute: Resolved

Desmos: [Vector Projections | Desmos](#)



Inclined Planes

GeoGebra: [Inclined plane forces – GeoGebra](#)



The image shows a GeoGebra window titled "INCLINED-PLANE FORCE VECTORS". The main area displays a blue inclined plane at an angle θ to the horizontal. A yellow block is on the plane. A white arrow labeled $-mg$ points vertically downwards from the center of the block. Two yellow arrows represent the components of gravity: $mg \sin(\theta)$ pointing down the plane and $-mg \cos(\theta)$ pointing perpendicular to the plane. A yellow arrow labeled F_{normal} points perpendicular to the plane, upwards and to the left. A dashed line shows the vertical projection of the block's position. The interface includes a toolbar with a mouse cursor and a zoom tool, and a control panel on the right with sliders for scale (0.3), μ (0), loc (5.4), and θ_{ramp} (0.61), and a checked "Show angles" option. Below the control panel are the coordinate system definitions and the force equations.

INCLINED-PLANE FORCE VECTORS

scale = 0.3
 $\mu = 0$
loc = 5.4
 $\theta_{\text{ramp}} = 0.61$
 Show angles

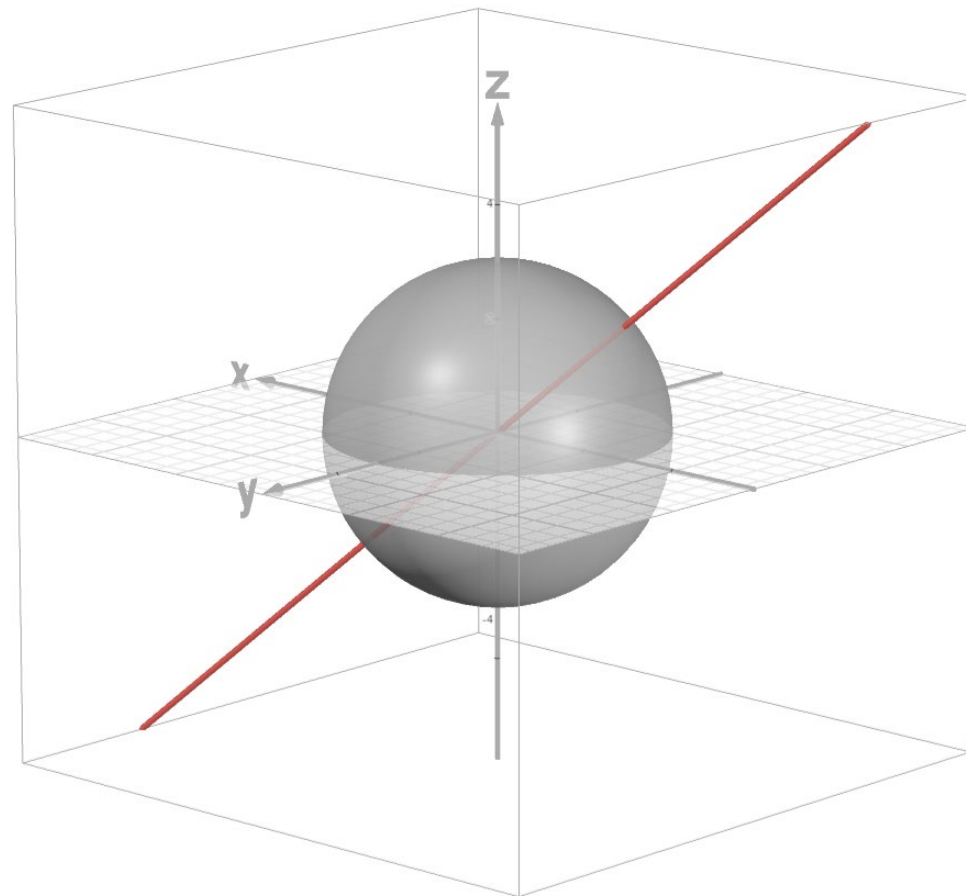
x: positive downward, \parallel to ramp
y: positive upward, \perp to ramp

$$F_{\text{down-ramp}} = m g \sin(\theta)$$
$$F_{\text{normal}} = m g \cos(\theta)$$
$$F_{\text{friction}} = -\mu F_{\text{normal}}$$

Visualising 3D objects

Desmos: <https://www.desmos.com/3d/09de2f64a5>

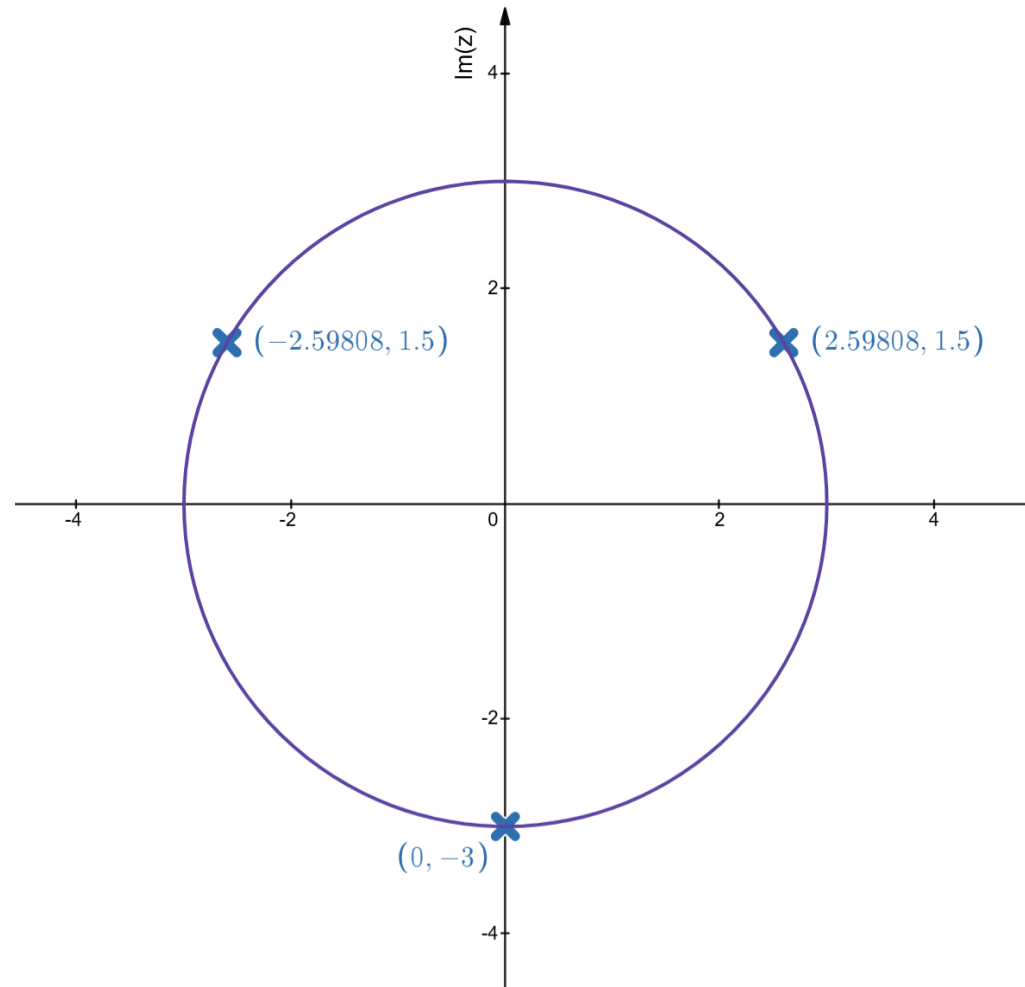
- Desmos 3D can be used to support students understanding objects in 3D. This includes spheres, planes, and lines.



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Roots of complex numbers

Desmos: <https://www.desmos.com/calculator/gpbqtruer1>

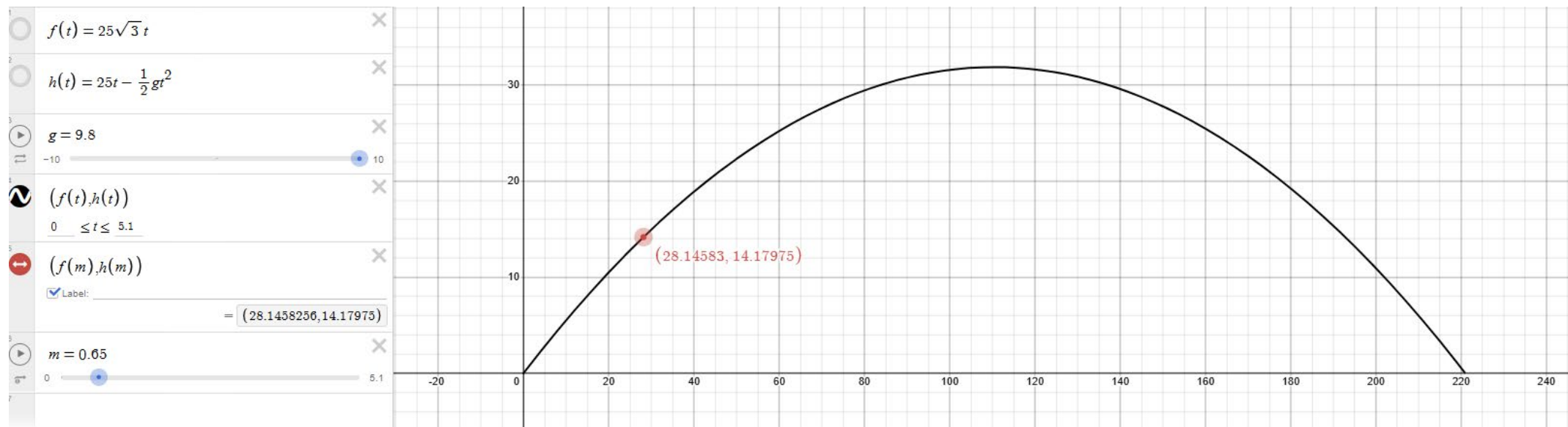


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Projectile motion

Desmos <https://www.desmos.com/calculator/quly6uy4yw>

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Probability density functions

- Connecting 'histogram' to probability density function.
- Area under the curve of $f(x)$ represents probability.
- $F(x) = \int_a^x f(t) dt$
- The shape, domain and behaviour of $F(x)$.
- The expected value of $f(x)$ and centre of mass.

Riemann sums and Trapezoidal rule:

- Desmos: <https://www.desmos.com/calculator/sezwq775wg>

Frequency histogram:

- Desmos: <https://www.desmos.com/calculator/w5dj2x3n8b>

Mixed concepts:

- Desmos: <https://www.desmos.com/calculator/ede49bb4f0>

Binomial distribution

- What does X represent? How do we interpret this?
- Probability distributed across all possible outcomes.
- Probability of r successes in n independent trials.
- Varying the parameters n and p . How does this affect the distribution?
Does this agree with our intuition?

Visualising the Binomial distribution:

- Desmos: <https://www.desmos.com/calculator/wvhka4reyp>

Expected value:

- GeoGebra: <https://www.geogebra.org/m/umhJzKsm>

Final thoughts: A recap

- Questioning can be used to guide students towards understanding.
- Examples of questioning strategies used to engage students and promote thinking:
 - "What do you observe/notice about...?"
 - "Does anyone notice any patterns?"
- Positioning students to develop their own understanding. Students can actively participate in meaning construction.
- Discussions about mathematics and ideas enables students of all abilities to participate.
- Engage students' and teachers' natural curiosity. Encourage students to ask 'Why?'.

A quick note

The resources that I have shared are not entirely my own. Thank you to everyone who has created and shared their resources. These have only enriched the teaching and learning of mathematics.

Visualising the Binomial distribution:

- This is not my creation. I have adjusted the original so that this is easier for me to use and to focus on the concepts I would like to discuss.

Expected value:

- This has been shared in its original form. I have not adjusted this.

Riemann sums and Trapezoidal rule:

- This has been shared in its original form. I have not adjusted this.

Frequency histogram:

- This has been shared in its original form.

Mixed concepts:

- I have adjusted a Desmos graph that looked at the link between a frequency histogram and a pdf.